Plasmon-exciton polaritons in two-dimensional semiconductor/metal interfaces

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The realization and control of polaritons is of paramount importance in the prospect of novel photonic devices. Here, we investigate the emergence of plasmon-exciton polaritons in hybrid structures consisting of a twodimensional transition-metal dichalcogenide (TMDC) deposited onto a metal substrate or coating a metallic thin film. We determine the polaritonic spectrum and show that, in the former case, the addition of a top dielectric layer and, in the latter case, the thickness of the metal film can be used to tune and promote plasmon-exciton interactions well within the strong-coupling regime. Our results demonstrate that Rabi splittings exceeding 100 meV can readily be achieved in planar dielectric/TMDC/metal structures under ambient conditions. We thus believe that this Rapid Communication provides a simple and intuitive picture to tailor strong coupling in plexcitonics with potential applications for engineering compact photonic devices with tunable optical properties.

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Introduction. Two-dimensional (2D) materials [1] have been the subject of increasing interest in nanophotonics due to their ability to host a large variety of polaritons [2,3], including gate-tunable plasmon polaritons in graphene [4–7] or phonon polaritons in hexagonal boron nitride (hBN) [8–10]. More recently, exciton polaritons in atomically thin semiconductors, such as transition-metal dichalcogenides (TMDCs) have also been observed experimentally [11–13], thus further expanding the current 2D "polaritonic library."

Excitons-electron-hole pairs bounded through their mutual Coulomb interaction-in 2D materials exhibit high binding energies when compared with excitons in conventional three-dimensional (3D) semiconductors. This fact is a direct consequence of the modification of the Coulomb potential in two dimensions, which results in less screening and thereby higher excitonic binding energies [14]. Therefore, excitons in 2D TMDCs strongly affect their electromagnetic response and light-matter interactions even at room temperature. For this reason, atomically thin TMDCs are currently emerging as viable platforms for studying strong coupling under ambient conditions. Indeed, strong coupling and mode hybridization of excitons in 2D materials with photonic cavity modes [12,15] and with plasmonic resonances [16-18] have been reported recently. These advances have thus unambiguously placed TMDCs on the map as suitable candidates for emerging quantum technologies [19] relying on strong coupling and coherent quantum control and can be viewed as potential alternatives to (or used in conjunction with) typical systems, such as J aggregates of organic dye molecules or quantum dots. In this context, whereas promoting exciton-photon interactions in photonic cavities may have the advantage of rendering lower losses, this comes at the expense of larger modal volumes when compared with plasmonic systems. On the other hand, the latter, despite exhibiting more losses, can deliver strong optical confinement and enhance light-matter interactions on the nanometer scale. This feature is pivotal, for instance, for achieving strong-coupling regimes at the single molecule level [20].

In this Rapid Communication, we theoretically investigate plasmon-exciton coupling in planar structures consisting of an atomically thin TMDC crystal deposited onto a metal substrate as depicted in Fig. 1(a). Upon resonant excitation, excitons can be created in the TMDC, whereas the metal can sustain surface-plasmon polaritons (SPPs). Hence, in a system composed of two such materials, the interaction between the individual excitations gives rise to hybrid plasmon-exciton polaritons. When the system is driven into the strong-coupling regime, energy can be exchanged coherently between the two eigenstates of the compound system. The signature of this phenomenon typically manifests itself in the optical spectra in the form of a Rabi splitting together with the emergence of anticrossing behavior in the polaritonic dispersion diagram. Here, we show that strong coupling between excitons and plasmons can be achieved readily in elementary dielectric/TMDC/metal interfaces by appropriately choosing the dielectric constant of the superstrate, or alternatively, the thickness of a TMDCcoated metal thin film. We compute the full plasmon-exciton polariton spectrum and retrieve the ensuing Rabi splitting, which we then feed into a coupled oscillator model (COM) for comparison. Our results demonstrate that Rabi splittings in excess of 100 meV can be achieved in such systems at room temperature. Finally, as an application of our theoretical results, we consider an experimental setting in which plasmonexciton polaritons are excited by exploiting the attenuated total reflection (ATR) technique in the so-called Otto configuration [4]. The corresponding results plainly show the manifestation of strong coupling in which the two hybrid modes are well

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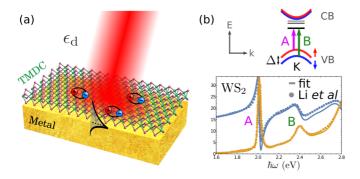


FIG. 1. (a) Illustration of the dielectric/TMDC/metal system under consideration in this Rapid Communication. (b) Scheme of a TMDC electronic structure around the *K* point, showing optical transitions from the spin-orbit split valence band to the exciton ground state (dubbed *A* and *B* excitons). Also plotted is the dielectric function data of WS₂ measured by Li *et al.* [21] together with the corresponding Lorentz oscillator fit $\epsilon_{WS_2}(\omega) = \epsilon_{\infty} + \sum_j f_j / (\omega_j^2 - \omega^2 - i\omega\gamma_j)$ (see Ref. [22] for details on the parameters).

separated according to the standard Rabi splitting to linewidth criterion [23]. We believe our Rapid Communication can be used as a springboard to tailor plasmon-exciton interactions in 2D materials interfacing 3D metallic structures, potentially opening new avenues to engineer the interplay between light and matter on the nanoscale.

Theory and results. The dispersion relation for polaritons sustained at a dielectric/TMDC/metal interface, such as the one portrayed in Fig. 1(a), directly follows from the implicit condition [4,7],

$$\frac{\epsilon_{\rm d}}{\kappa_{\rm d}} + \frac{\epsilon_{\rm m}}{\kappa_{\rm m}} = \frac{\sigma_{\rm 2D}}{i\omega\epsilon_0},\tag{1}$$

where $\kappa_i^2 = q^2 - \epsilon_j \omega^2 / c^2$ with $j = \{d, m\}$. Here, ϵ_d stands for the relative permittivity of the upper dielectric, and $\epsilon_{\rm m}(\omega)$ represents the metal's complex dielectric function. The electromagnetic properties of the 2D TMDC are accounted for via the material's (surface) conductivity $\sigma_{2D}(\omega)$. In what follows, and for the remainder of the Rapid Communication, we consider the metal substrate to be made of gold, and the 2D TMDC to be a monolayer of tungsten disulfide (WS_2) . The reason is that the latter exhibits excitonic resonances with strong oscillator strengths [21], whereas the former is a widely used plasmonic medium. Furthermore, in order to obtain results that are faithful in the most possible way to realistic experimental conditions, we model gold via its experimentally obtained dielectric function [24]. Similarly, we construct the 2D conductivity of the WS₂ monolayer out of the dielectric function data measured by Li et al., to which a Lorentz oscillator has been fitted [21]—see also Fig. 1(b) for details. In particular, we take $\sigma_{2D}(\omega) = -i\omega\epsilon_0 d[\epsilon_{TMDC}(\omega) - 1]$ where d is an effective thickness, typically the material's bulk interlayer spacing ($d_{WS_2} = 6.18$ Å for WS₂) [21]. As Fig. 1(b) portrays, the WS₂ dielectric function is dominated by two resonances attributed to its A and B excitons, corresponding to optical transitions between the spin-orbit split valence band and the n = 1 exciton state. For a detailed account of the exciton properties in 2D TMDCs, see Ref. [25].

In possession of the materials' response functions, the polaritonic spectrum stems from the numerical solution of Eq. (1)in the $(q, \hbar \omega)$ phase space. Figure 2 shows the dispersion diagram of plasmon-exciton polaritons in three dielectric/WS₂/Au structures with different capping dielectrics. The bare SPP dispersion in a dielectric/Au interface is also plotted and serves as a guide to the eyes. It is apparent from the figure that plasmon-exciton hybridization arises in the neighborhood where the uncoupled SPP crosses the energy of the A exciton. Since we solve Eq. (1) by feeding in a real frequency, the corresponding numerical solution yields a complex-valued q (whose real part is plotted in Fig. 2), and thus a backbending or anomalous dispersion behavior emerges rather than the usual anticrossing [4,13] (the more familiar anticrossing presents itself in experiments at fixed angles and varying excitation energies; we will consider this case below). We note that such a back bending is an unambiguous signature of strong coupling [26]. Additionally, the inset in each panel in Fig. 2 displays zoomed versions of the area where such mode hybridization occurs. The span of the insets' vertical axes is the same to facilitate the comparison of the Rabi splitting between panels. Figure 2 clearly shows that the Rabi splitting energy (indicated by the arrows) significantly increases as the dielectric constant of the cladding dielectric gets larger. Incidentally, our calculations have shown that for an air/WS₂/Au planar structure the Rabi splitting is almost absent. However, Fig. 2 demonstrates that the addition of a dielectric top layer can be used to substantially enlarge its value. In fact, the Rabi splitting energy increases from a barely tangible $\hbar\Omega_{\rm R} = 24$ meV for $\epsilon_{\rm d} = 3$ in Fig. 2(a) to a striking value of $\hbar\Omega_{\rm R} = 73$ meV for $\epsilon_{\rm d} = 9$ in Fig. 2(c). With the purpose of both validating the numerically retrieved Rabi splittings and in the interest of providing physical insight, we have introduced these as parameters on the COM, which is widely adopted in the literature to describe strong coupling [12,16,17,23]. Within the COM framework, the frequencies of the two hybrid modes read (neglecting damping to simplify the analysis)

$$\omega_{\pm}(q) = \frac{\omega_{\rm pl}(q) + \Omega_{\rm ex}}{2} \pm \frac{1}{2} \sqrt{[\omega_{\rm pl}(q) - \Omega_{\rm ex}]^2 + \Omega_{\rm R}^2}, \quad (2)$$

where $\omega_{pl}(q)$ refers to the bare SPP dispersion [obtained from Eq. (1) with $\sigma_{2D} \rightarrow 0$] and $\hbar \Omega_{ex}$ is the A exciton energy. The comparison of the plasmon-exciton dispersion and corresponding $\hbar\Omega_{\rm R}$ determined numerically with the analytical results from the COM reveals an outstanding agreement as can be seen from the insets in Fig. 2. Augmenting the previous results to a larger set of dielectric claddings, one can construct a map of the Rabi splitting as a function of ϵ_d . The outcome of such a procedure is shown in Fig. 3. As discussed above, the Rabi splitting energy increases monotonically upon increasing the relative permittivity of the top dielectric medium (see the Supplemental Material [27] for a detailed analysis). These results can be understood by noting that, for a Drude metal (for the sake of clarity), the nonretarded surface-plasmon frequency is given by $\omega_{\rm sp} = \omega_{\rm p}/\sqrt{1+\epsilon_{\rm d}}$. In typical metals, such a resonance lies well above the energy of excitons in TMDCs, and consequently the corresponding plasmon-exciton coupling is weak. Yet, as one increases the permittivity of the dielectric, ω_{sp} undergoes a redshift and approaches the excitonic resonance thereby promoting successively stronger

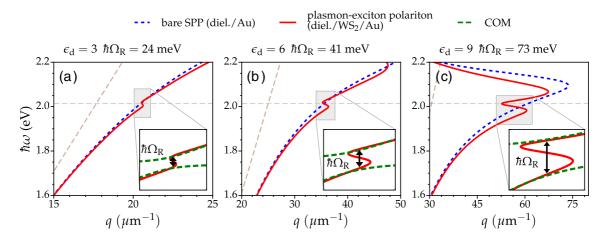


FIG. 2. Dispersion relation $\hbar\omega$ versus Re{q} of plasmon-exciton polaritons in dielectric/WS₂/Au structures (the red solid lines) with different top dielectrics as indicated at the top of each panel. The dispersion of the SPP in the corresponding dielectric/Au interfaces is also plotted (the blue dashed lines) along with the energy of the WS₂ exciton A (the horizontal dashed line) and the light lines (the dashed lines in light brown). The insets in each panel show a zoom of the area around the mode back-bending/anticrossing together with the Rabi splitting (marked by the arrows). The retrieved Rabi splitting energies are shown at the top of each panel and were used as a parameter in the analytical COM, whose result (up to a minute absolute vertical shift) is depicted by the green dashed lines in the insets.

plasmon-exciton interactions. Accordingly, the corresponding mode hybridization also occurs at larger q's so that a higher proportion of the field distribution lies in the vicinity of the 2D excitonic medium (i.e., the spatial overlap between the field of the SPP and the exciton increases). In previous experiments, a similar tuning is carried out by depositing metallic nanoparticles (NPs) on the 2D material so that the plasmon resonance is controlled alternatively by changing the NPs' size [16–18]. The advantage of our approach is that it eliminates the necessity of nanostructuring. Our results therefore demonstrate the ability to achieve plasmon-exciton strong coupling at room temperature in simple and highly scalable dielectric/TMDC/metal configurations.

We now consider an application of our results, namely, the excitation of plasmon-exciton polaritons via prism coupling using the ATR technique. In this scenario, the system's polaritons can be excited by the evanescent waves coming out of a prism placed on top of the dielectric/WS₂/Au structure (i.e., photons can "tunnel" from the prism to the WS₂/Au interface

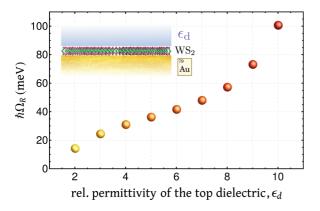


FIG. 3. Rabi splitting energy (in meV) as a function of the dielectric constant of the top insulator in dielectric/WS₂/Au structures.

through the dielectric layer). All our calculations relative to the ATR configuration were performed using the transfer-matrix method (see Ref. [4] for more information on this technique). Figure 4(a) depicts the ATR signal that would be obtained in experiments carried out at distinct incident angles. For any of the angles considered, two minima can readily be observed in the ATR spectra, corresponding to the two branches of the plasmon-exciton dispersion relation. Note that, as we have mentioned above, in spectroscopic measurements at fixed

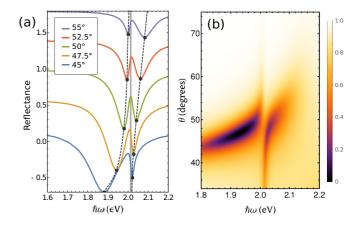


FIG. 4. Reflectance spectra in an ATR configuration. (a) ATR spectra collected at different incident angles. The two uppermost (bottommost) curves are shifted vertically by 0.4 (-0.4) each in the interest of clarity. (b) Two-dimensional plot of the reflectance in an ATR experiment for arbitrary incident angles and excitation energies. The avoided crossing between each polariton branch can clearly be seen around the *A* exciton energy at $\hbar\Omega_{ex} = 2.014$ eV. Parameters: $\epsilon_d = 5$, L = 90 nm (dielectric layer thickness), and $\epsilon_{prism} = 16$. We have halved the exciton γ_j 's used thus far to simulate the effect of reducing the temperature (nevertheless, the general features remain essentially unchanged at room temperature, save for a slight increase in the linewidths).

momenta (here given by the angle $q = \frac{\omega}{c} \sqrt{\epsilon_{\text{prism}}} \sin \theta$), the strong coupling manifests itself in the traditional form of an avoided crossing together with the transfer of spectral weight between the two polariton branches as the angle is varied—see Fig. 4. Moreover, Fig. 4(b) illustrates the dependence of the reflectance on both the incident angle and the excitation energy. In this regard, each of the curves presented in Fig. 4(a) simply corresponds to horizontal cuts in Fig. 4(b) at the selected angles. In addition, the two minima recognized in the former occur at the energies where such horizontal lines cross each one of the two hybrid plasmon-exciton modes visible in the latter. We stress the similarities between the spectra portrayed in Figs. 2 and 4(b) after a reflection with respect to the origin since these are nothing but two alternative ways to present the polaritonic spectrum.

Tuning the plasmon-exciton interaction using thin films. We further note that an alternative possibility to achieve and tailor the plasmon-exciton interaction in TMDC/metal planar structures is to consider a metallic thin film instead of a semiinfinite metal substrate. In such a scheme, the key role played by the dielectric superstrate in tuning the strong coupling is now played by the thickness of the thin film. In particular, a dielectric/TMDC/metal/TMDC/dielectric structure sustains two modes of opposite symmetries that are thickness dependent. Focusing on the low-frequency mode [28], the corresponding spectrum stems from the solution of [4,29]

$$\tanh(\kappa_{\rm m}t/2)\frac{\epsilon_{\rm m}}{\kappa_{\rm m}} + \frac{\epsilon_{\rm d}}{\kappa_{\rm d}} = \frac{\sigma_{\rm 2D}}{i\omega\epsilon_0},\tag{3}$$

where t denotes the thickness of the metallic film. In the above, we have assumed a symmetric dielectric environment for the sake of clarity alone. Figure 5(a) depicts the numerical solution of Eq. (3) for a representative structure composed of a WS_2 -coated gold film embedded in a medium with dielectric constant $\epsilon_d = 2.1$ (e.g., SiO₂). The four curves show the dispersion diagrams calculated for thin-film thicknesses varying from 40 to 10 nm. Clearly, despite the low-index dielectric with just $\epsilon_d = 2.1$, large Rabi splittings can now readily be achieved by controlling the metal thickness. The magnitude of the Rabi splitting as a function of the Au film thickness is illustrated in Fig. 5(b) with the cases plotted in the upper panel highlighted using the same colors. Indeed, in those cases, the obtained energy splittings grow from an already significant value of 40 meV up to about 100 meV. In contrast, using the same dielectric medium to encapsulate a thick gold substrate covered with WS₂, as in the initial case, one would only obtain a Rabi splitting of about 15 meV [as indicated by the dashed line in Fig. 5(b)]. Therefore, these results highlight the benefit of exploiting the thickness-dependent low-frequency SPP mode of metallic thin films to tailor the plasmon-exciton coupling in planar structures, which are straightforward to fabricate in an experimentally convenient fashion.

Conclusions. In conclusion, we have investigated the emergence of plasmon-exciton polaritons in heterostructures consisting of dielectric/TMDC/metal vertical stacks. Throughout the Rapid Communication, we have focused on the case where the TMDC was a WS₂ monolayer thanks to its strong exciton oscillator strengths and where the metal was gold, whose chemical stability has endowed it as a popular plasmonic material. Nevertheless, our treatment and subsequent analysis

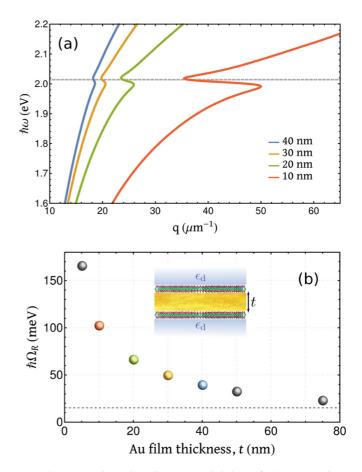


FIG. 5. (a) Dispersion diagram (Re{q}, $\hbar\omega$) of plasmon-exciton polaritons in dielectric/WS₂/Au/WS₂/dielectric structures with varying film thicknesses. The horizontal dashed line indicates the resonance of the *A* exciton at $\hbar\Omega_{ex} = 2.014$ eV. The corresponding Rabi splittings are $\hbar\Omega_R = 39$, 49, 66, 101 meV in order of decreasing thickness. (b) Rabi splitting energy (in meV) as a function of the Au thin-film thickness in WS₂-coated Au films embedded in a homogeneous dielectric medium with $\epsilon_d = 2.1$. The colored spheres correspond to the cases plotted in the top panel with matching colors. The horizontal dashed line indicates the $t \rightarrow \infty$ limit (corresponding to a thick Au substrate). In both panels we have used the experimentally obtained optical constants of Au [24] and of WS₂ [21].

can be generalized straightforwardly for any 2D TMDC/metal pair. Our results plainly demonstrate the emergence of a plasmon-exciton interaction within the strong-coupling regime upon adequately choosing the dielectric environment enclosing the TMDC/metal structure or the thickness of the metal film in a double interface configuration. Furthermore, we have shown that the Rabi splitting is enlarged as the relative permittivity of the dielectric layer increases. This behavior can be interpreted easily by noting that, for an air/metal interface, the corresponding ω_{sp} lies well above the exciton resonances of TMDCs. Notwithstanding, the placement of a top dielectric layer effectively reduces the nonretarded surface-plasmon resonance thereby successively increasing the spectral overlap between the plasmon and the exciton modes as $\epsilon_{\rm d}$ is increased. Moreover, besides the single-interface case, we also have considered a gold thin film coated with a 2D TMDC and encapsulated in a homogeneous dielectric medium. We have demonstrated that this latter configuration constitutes a convenient alternative to the former since the magnitude of the Rabi splitting can be customized upon varying the thin-film thickness, which in turn can be controlled experimentally with precision.

Our calculations predict that Rabi splitting energies in excess of $\hbar \Omega_{\rm R} = 100$ meV can be achieved comfortably even at room temperature, which makes our structures viable alternatives to the J aggregates of organic molecules or quantum dots as platforms for studying strong coupling. Remarkably, we also have found that the Rabi splittings stemming from the dielectric/WS₂/Au vertical structures considered here are comparable or even surpass the ones reported in experiments with plasmonic NPs deposited on TMDCs [16-18] or for TMDCs inside photonic cavities [12,15]. All of this with the added advantage of, in comparison, being extremely easy to fabricate on larger scales. Towards an experimentally oriented study, we also have computed the reflectance measured in a typical ATR experiment in which plasmon-excitons are excited via prism coupling. Here too, our results-embodied in Fig. 4-reveal the existence of strong plasmon-exciton interactions within the strong-coupling regime. In passing, the resemblance between the spectra exhibited in Fig. 4(a) with the spectral features akin to strong coupling between plasmons in graphene nanostructures and phonons of the underlying substrate (e.g., hBN or SiO₂) [30–32] is worth mentioning.

Lastly, it should be mentioned that in our description we have neglected the impact of the dielectric environment surrounding the TMDC on the exciton resonances. It is well known that a landscape with higher permittivity leads to increased screening. The effect is twofold: It decreases both the quasiparticle band gap and the exciton binding energy and thus influences the excitonic resonance [14,25,33,34]. In previous

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studies the overall effect seems to be small for our purposes (since both effects work against each other) [33] especially where the A exciton is concerned, and therefore we do not take them into account here. However, to what extent that remains valid when the screening is due to an adjacent metal (with much higher permittivity) remains an open question since to the best of our knowledge such a study is still lacking in the literature. A possible way to mitigate the impact of the screening by the metal would be to include a thin dielectric layer between the metal and the TMDC. Our calculations show [27] that the corresponding Rabi splitting only is decreased slightly and that can be even compensated by increasing ϵ_d or decreasing t. Nonetheless, we expect that our results and the ensuing analysis to be robust against that effect since we anticipate its consequence to be only a shift in the (absolute) position of the excitonic resonances. Furthermore, we believe that the simplicity is the main merit of our description together with its intuitive account of the plasmon-exciton interaction.

We believe that our Rapid Communication contributes to the active pursuit of novel plexcitonic architectures based on hybrid 2D/3D structures made from atomically thin semiconductors and 3D metals. Our findings show that these platforms can be used as test beds to investigate plasmon-exciton interactions in the strong-coupling regime, setting the stage for future ultracompact nanophotonic devices operating at room temperature.

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